

**CSCI 241H:**  
**HOMEWORK 5**

Show your work.

1. If I tell you that the running time of my program is at least  $O(f(x))$ , why is this statement meaningful?
2. Let  $f(x)$  be  $O(g(x))$  and  $g(x)$  be  $O(h(x))$ . Show that  $k(x) = 3f(x) + 5g(x) + 8h(x)$  is  $O(h(x))$ .
3. Consider the series  $f(k) = \sum_{i=1}^k 2k - 1$ . Show that  $f(k) = k^2$ . Don't look at any resources please.
4. Let  $0 < x < 1$ . Show that the infinite summation  $x + x^3 + x^5 + x^7 + \dots$  evaluates to  $x/(1 - x^2)$ .