

**CSCI 241H:
HOMEWORK 2**

Show your work.

1. Write the following in predicate logic. Don't forget the quantifiers; explain what each predicate means.
 - (a) Every student who takes 241 either comes to class regularly, or borrows the notes from someone who comes to class regularly.
 - (b) There is no one in the world who is loved by everybody.
 - (c) There is such a man in this group that no one is taller than he is.

2. Show that

$$\forall xP(x) \vee \forall xQ(x) \neq \forall x(P(x) \vee Q(x))$$

3. Are the following two expressions equivalent? Argue.

$$\forall x(P(x) \rightarrow Q(x))$$

and

$$(\forall xP(x)) \rightarrow (\forall xQ(x))$$

4. Page 80, question 35 from your book:

If Superman were able and willing to prevent evil, he would do so. If Superman were unable to prevent evil, he would be impotent; if he were unwilling to prevent evil, he would be malevolent. Superman does not prevent evil. If Superman exists, he is neither impotent nor malevolent. Therefore, Superman does not exist.