Shadows of meaning

Chung-chieh Shan Cornell University

21 December 2011



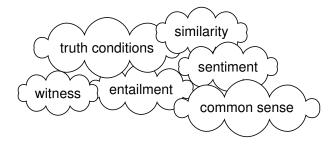
What is meaning?

. . .

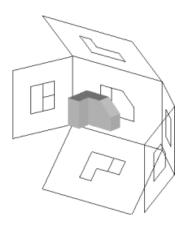
Semantics with no treatment of truth conditions is not semantics.

In order to say what a meaning is, we may first ask what a meaning does, and then find something that does that.

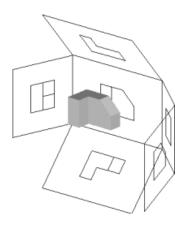
-Lewis "General semantics"



Informative shadows from random projections



Informative shadows from random projections

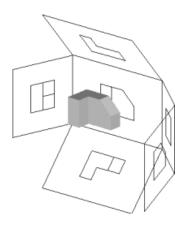


Hope in progress that "meaning" is not so polysemous:

- 1. Generics about kinds as topological spaces
- 2. Distributional semantics from language models

Reconstruct non-just-so stories from projections.

Informative shadows from random projections



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Generic statements refer to kinds (Carlson)

Lions are carnivores. Lions have four legs. Lions have manes. Lions give birth to live young. Lions roar. Lions are female. (not) Lions are widespread.

Lions are extinct. (not)

Not universal, not existential, not proportional, not quantificational.

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Lions are widespread. Lions are extinct. (not)

Not universal, not existential, not proportional, not quantificational. What does it take for a kind to satisfy a property that applies to members of the kind?

Generic statements are default generalizations (Leslie)

See a few lions eat flesh, then encounter a new lion.

See a few lions give birth to live young, then encounter a new lion.

See a few lions that are male, then encounter a new lion.

See a few lions at the zoo, then encounter a new lion.

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Tolerate negative counterexamples

Lions are female. (not) *Peacocks have big blue tails.* (not if females had big pink tails)

- Generalize along characteristic dimensions Birds lay eggs.
 Bees reproduce. Bees are not sterile.
- Consider the function and purpose of artifacts
 OrangeCrusher 2000s crush oranges. (even if never used)
 Firefighters extinguish fires. (even if no fires)
- Sense disposition for disease, disaster, danger, disgust Mosquitoes carry the West Nile virus. Sharks attack bathers.

From cognition to logic

Logic is good for formalizing statements and their idealized inference patterns.

Predicate logic is good for formalizing quantified statements.

What is good for formalizing generic statements?

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What is good for formalizing generic statements?

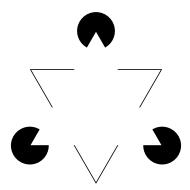
Adam Bjorndahl, Will Starr and I propose to use topology:

- Kinds are topological spaces
- Generic properties are large sets

One notion of large sets is what mathematicians call generic-



Kanizsa's subjective contours



Lining up is robust, not an accident: it holds after jiggling





Views show three points.

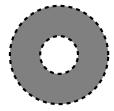
A topological space is

- a set X of points, and
- certain sets of points designated as open.

(Unions and finite intersections of open sets must be open.)

•
$$X = \mathbb{R}^2$$

$$\begin{array}{l} \blacktriangleright \ U \subseteq X \text{ is open iff} \\ \forall p \in U, \ \exists \epsilon > 0, \ \forall q \in X, \ d(p,q) < \epsilon \ \rightarrow \ q \in U \end{array}$$





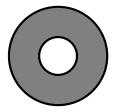
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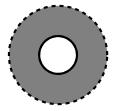
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Example: metric spaces, for instance

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 is open iff

 $orall p\in U, \;\; \exists \epsilon>0, \;\; orall q\in X, \;\; d(p,q)<\epsilon \;\; o \;\; q\in U$

Example: partial orders, for instance

• X =strings

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(Kripke models)

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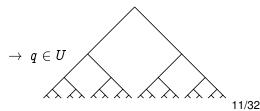
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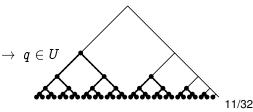
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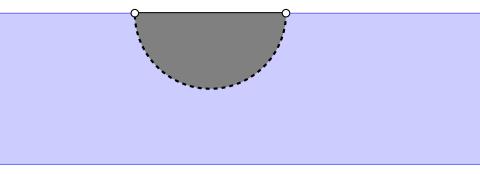
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What are the points? At least the actual lions. Maybe also metaphysically possible lions. But not just.

Points are like situations or discourse contexts:

- Points may be situations or discourse contexts.
- Points reflect how human cognition carves up the world.
- The metaphysical status of points is unclear.
- One can worry too much about points. (as with viewpoints and individuals)

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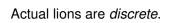
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A property is a set of points.

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Neither-male-nor-female points are *dense*.

Kinds are topological spaces

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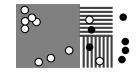
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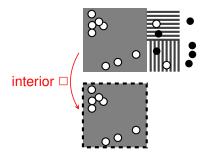


Intensionality arises from the extra points and their topology-

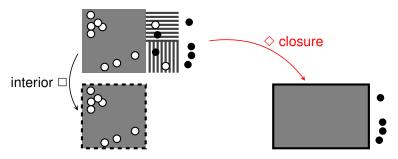
A qualitative yet geometric notion of nearness.



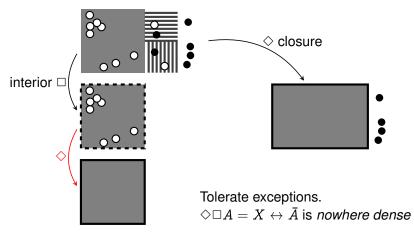
A qualitative yet geometric notion of nearness. Gives operations:

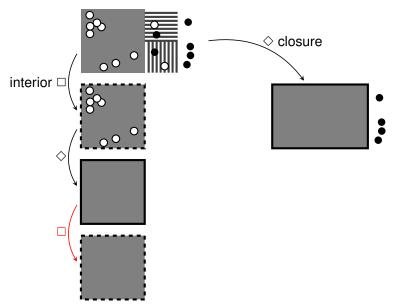


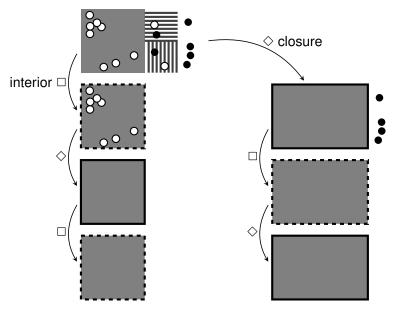
 $\Box A = A \leftrightarrow A$ is open Where A holds robustly, locally.



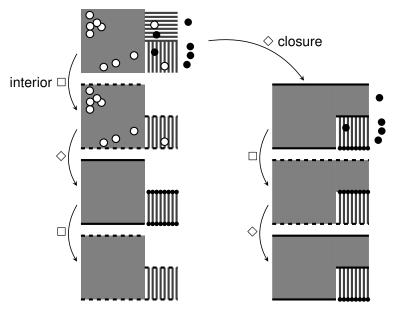
 $\Diamond A = A \leftrightarrow A \text{ is closed}$ $\Diamond A = X \leftrightarrow A \text{ is dense}$







A qualitative yet geometric notion of nearness. Gives operations:



A set of points is a property. An open set is a "positive" (Leslie), "human-graspable" (Kratzer) property.

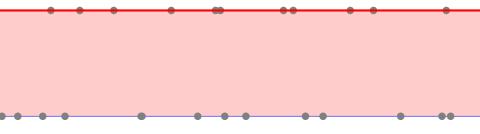
These properties are sensible grounds for similarity claims:

Lions are like tigers because they both have paws. # Tigers are like snakes because they both do not have manes. Tweetie is like Lulu because they both are ravens/black. # Fido is like Quincy because they both are not ravens/black.

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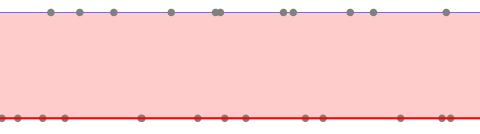
Breathing room

A set of points is a property. An open set is a "positive" (Leslie), "human-graspable" (Kratzer) property.



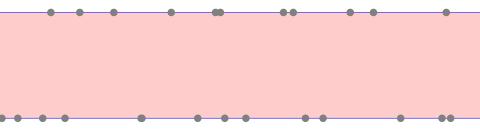
Lions have manes.

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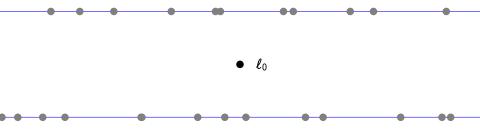
Lions give birth to live young.

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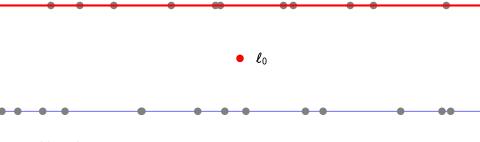


Lions have manes and give birth to live young.

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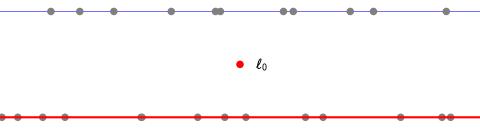


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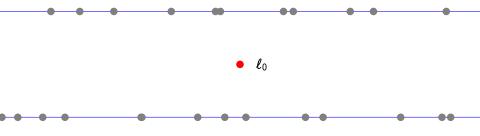
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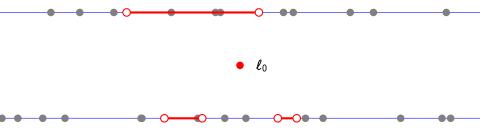
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Lions have manes and give birth to live young.

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Put ℓ_0 in every nonempty open set. In other words, let $\ell_0 \succeq$ every element of partial order. This generic lion ℓ_0 may have properties that no actual lion has!

Add more points for generic statements about subkinds: $\ell_0 \succ \ell_f \succ$ every actual female lion. Just so?

Notions of largeness

	$ar{A}$ is nowhere dense $(X = \diamondsuit \Box A)$ $= \Box \diamondsuit \Box A)$	\bar{A} is <i>meager</i> (countable union of nowhere dense)	A is not meager
$\bigcirc A, \ \boxdot B \vDash \boxdot (A \cap B)$	\checkmark	\checkmark	
$\boxdot A \vDash \boxdot (A \cup B)$	\checkmark	\checkmark	
${}_{igodot}A_i \vDash {}_{igodot} \bigcap_{i=1}^\infty A_i$	×	\checkmark	
$\Box \emptyset \vDash \bot$	\checkmark	×	
Degenerates to ∀ in discrete space	\checkmark	×	
Preserved by restrictio to open subspace	n √	\checkmark	

We want to axiomatize \square separately from \square, \diamondsuit .

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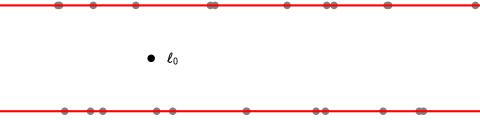
Positive alternatives and public announcement

Lions give birth to live young. Lions are female. (not)

Positive alternatives and public announcement

Lions give birth to live young. Lions are female. (not)

Maybe bringing up *male* or *female* restricts to the set $Male \cup Female$, not an open set in the original lion space. (In fact, its interior is empty.)



Generics and kinds: summary

Kinds are topological spaces.

- Points are not just actual individuals.
- Open sets are sensible properties.

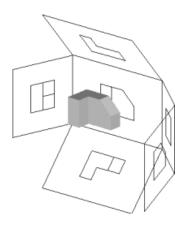
Generic properties are large sets.

► Inference patterns arise from □ = □◇□ and public announcement.

'But it has always happened that the more I hate men individually the more I love humanity.'

-Dostoyevski "The Brothers Karamazov"

Informative shadows from random projections



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Thanks

Bolzano

 European Masters Program in Language and Communication Technologies

Trento

- Marco Baroni
- Raffaella Bernardi
- Roberto Zamparelli

Rutgers

- Jason Perry
- Matthew Stone

Cornell

- John Hale
- Mats Rooth

Distributional semantics

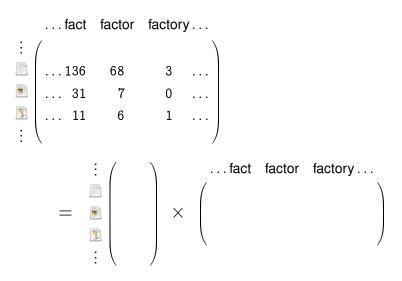
For information retrieval, bag of words in each document.

	fact	factor	factory	
÷	(
	136	68	3	
	31	7	0	
7	11	6	1	
:	()

Stopwords, stemming, tagging Normalize by document and by word Inner products for keyword/similarity retrieval (why does it work?)

Distributional semantics

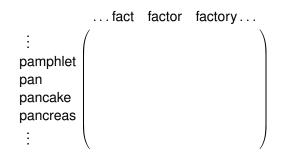
For information retrieval, bag of words in each document.



Reduce dimensionality—topic models

Distributional semantics

Rows are signs (phrases). Columns are contexts (nearby words).



All mixed up with world knowledge and pragmatic debris. But this shadow of meaning does do

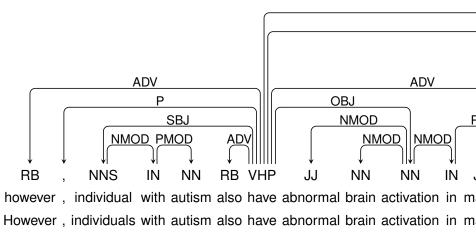
- similarity, relevance, analogy (inner product)
- entailment: lexical (feature inclusion), quantifier (?)
- sentiment

Two views: geometric (e.g., cosine distance) and probabilistic (e.g., KL divergence). See *information geometry*.

Perform different tasks without going back to the corpus? Phrase meanings? (sparse data; compositionality) Use syntactic structure? (word dependencies easier; sparse data)

RB , NNS IN NN RB VHP JJ NN NN IN whether a non-activation in m however , individual with autism also have abnormal brain activation in m

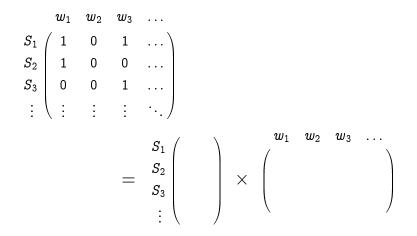
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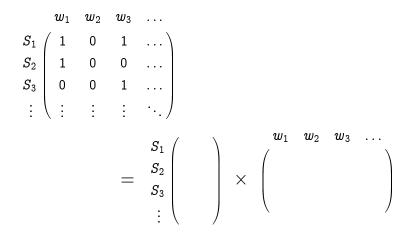
Rows are utterances. Columns are worlds and utterance contexts?

	w_1	w_2	w_3	•••
$S_1 \ S_2$	(1	0	1)
	1	0	0	
S_3	0	0	1	
÷	(:	÷	÷	·)

Rows are utterances. Columns are worlds and utterance contexts? Decomposition reveals entities?



Rows are utterances. Columns are worlds and utterance contexts? Decomposition reveals entities?



Rows are phrases. Columns include linguistic contexts?

From language model to distributional semantics

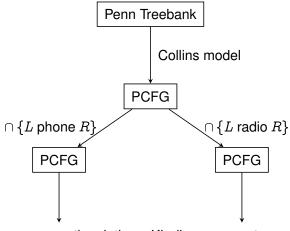
Sparse data motivates language modeling to produce virtual infinite corpus: not frequencies observed but probabilities estimated (smoothed, factored).

Let the distributional meaning of a phrase S be the probability distribution over its contexts C.

$$\llbracket S \rrbracket = \lambda C. \frac{\Pr(C[S])}{\sum_{C'} \Pr(C'[S])}$$
$$\llbracket \text{red army} \rrbracket = \lambda(L, R). \frac{\Pr(L \text{ red army } R)}{\sum_{(L', R')} \Pr(L' \text{ red army } R)}$$
$$\llbracket \text{red } S \rrbracket = \lambda(L, R). \frac{\llbracket S \rrbracket (L \text{ red}, R)}{\sum_{(L', R')} \llbracket S \rrbracket (L' \text{ red}, R')}$$

Probabilities from any model: bag of words, Markov, PCFG... Pass the buck.

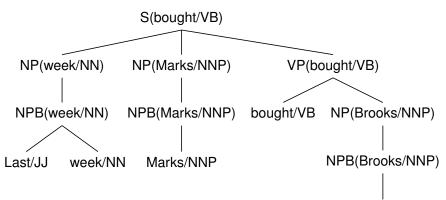
From Penn Treebank to distributional semantics



semantic relations, KL divergence, etc.

Collins model

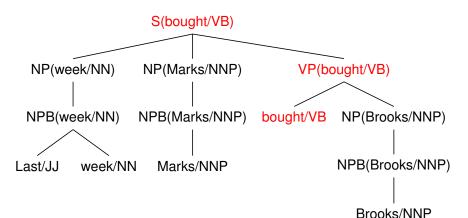
Lexicalized PCFG for parsing (1997) Not for generation (Post & Gildea 2008) Bikel (2004) exegesis



Brooks/NNP

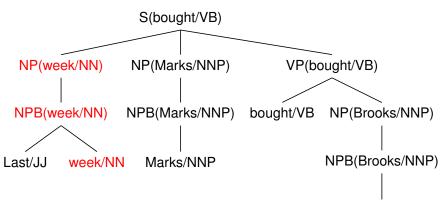
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Brooks/NNP

Summary statistics

Standard English training set: Wall Street Journal §§02-21

- 39832 sentences
- ▶ 950 028 word tokens
 - 44 113 unique words
 - 10 437 unique words that occur 6+ times
- 28 basic nonterminal labels
 42 parts of speech

Tiny for a corpus today.

Simplified Collins Model 1

 575 936 nonterminals 15 564 terminals 12 611 676 rules

Big for a grammar today.

. . .

Concept	Relation	Relatum	Baroni and Lenci Evaluation
phone phone phone phone phone phone phone phone phone phone phone phone	coord coord coord hyper hyper hyper hyper hyper hyper hyper mero mero	computer radio stereo television commodity device equipment good object system cable dial	 of Semantic Spaces (2011) Only head nouns observed in corpus: NP(phone/NN) NPB(phone/NN)
phone phone phone phone phone phone	mero mero mero random-n random-n random-n	number plastic wire choice clearance closing	Compute KL divergences among distributions over <i>modifier-nonterminal</i> <i>sequences</i>

. . .

Concept	Relation	Relatum	Baroni and Lenci Evaluation
phone phone phone phone phone phone phone phone phone	coord coord coord hyper hyper hyper hyper hyper hyper hyper mero	computer radio stereo television commodity device equipment good object system cable	of Semantic Spaces (2011) Only head nouns observed in corpus: NP(phone/NN) NPB(phone/NN) ← phone/NN
phone phone phone phone phone phone phone	mero mero mero random-n random-n random-n	dial number plastic wire choice clearance closing	Compute KL divergences among distributions over <i>modifier-nonterminal</i> <i>sequences</i>

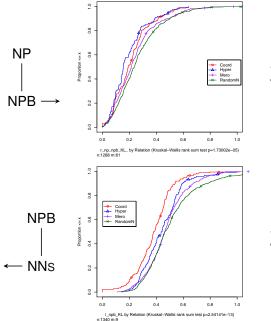
. . .

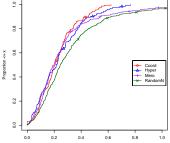
Concept	Relation	Relatum	Baroni and Lenci Evaluation
phone phone phone phone phone phone phone phone phone phone phone	coord coord coord hyper hyper hyper hyper hyper hyper hyper mero mero	computer radio stereo television commodity device equipment good object system cable dial	of Semantic Spaces (2011) Only head nouns observed in corpus: NP(phone/NN) NPB(phone/NN) → ← phone/NN
phone phone phone phone phone phone	mero mero mero random-n random-n random-n	number plastic wire choice clearance closing	Compute KL divergences among distributions over <i>modifier-nonterminal</i> <i>sequences</i>

38 Concept	Relation 68	7 Relatum	Baroni and Lenci Evaluation
phone 17	3 coord	computer	 of Semantic Spaces (2011)
phone	coord	radio	Only head nouns observed
phone	coord	stereo	•
phone	coord	television	in corpus:
phone 12	5 hyper	commodity	NP(phone/NN)
phone	hyper	device	
phone	hyper	equipment	
phone	hyper	good	NPB(phone/NN) →
phone	hyper	object	
phone	hyper	system	
phone 49	0 mero	cable	← phone/NN
phone	mero	dial	·
phone	mero	number	Compute KL divergences
phone	mero	plastic	among distributions over
phone	mero	wire	modifier-nonterminal
phone 56	1 random-n	choice	sequences
phone	random-n	clearance	0044011000
phone	random-n	closing	

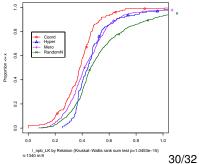
$D_{\rm KL}$ (Concept || Relatum)

$D_{\mathrm{KL}}(\mathrm{Relatum} \parallel \mathrm{Concept})$



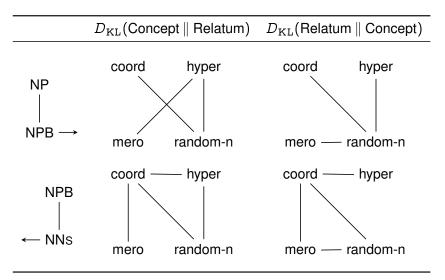


r_np_npb_LK_ by Relation (Kruskal-Wallis rank sum test p=5.88196e-06) n:1288 m:61

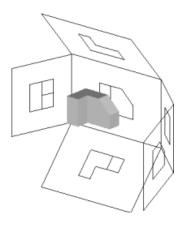


Mann-Whitney-Wilcoxon rank sum test

Edges indicate p < .01



Summary



Generics about kinds as topological spaces

 System 1 reasoning in discrete space is System 2 reasoning

Distributional semantics from language models

 Estimate felicity in context from observed use